

Mathematical modelling for malaria elimination

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Elimination versus control

- Control strategies target clinical disease
- Elimination strategies must target transmission
 - sub-clinical infection makes a significant contribution to transmission especially in high intensity settings
- The sparing use of new anti-malarial drugs has been recommended to minimize the selective pressure on the parasite

BUT

- Optimal elimination strategies may include use of anti-malarial drugs at high coverage
- Thus strategies designed to extend the lifespan of chemotherapies conflict with those required to successfully and rapidly eliminate the disease



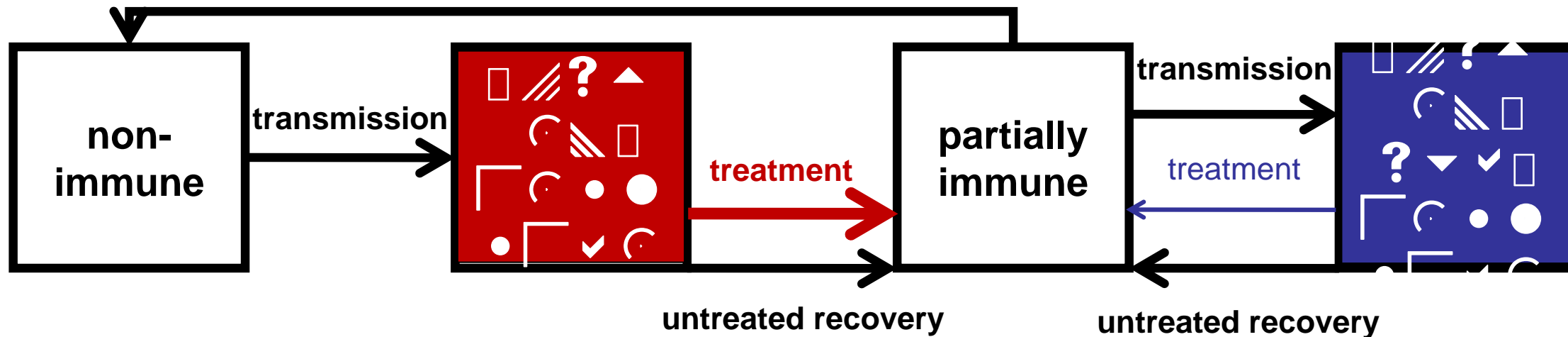
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A simple model structure

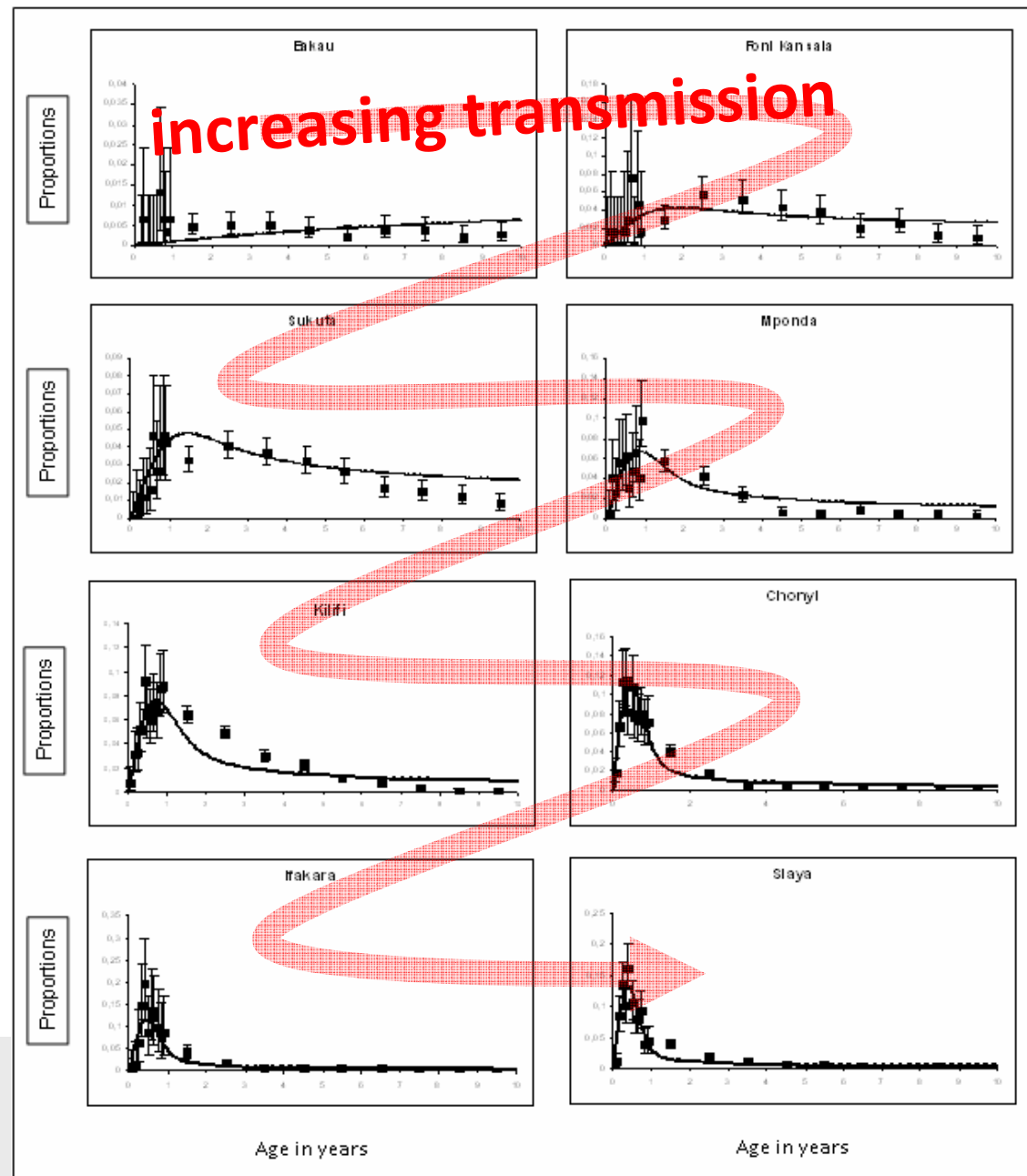
loss of immunity in the absence of challenge



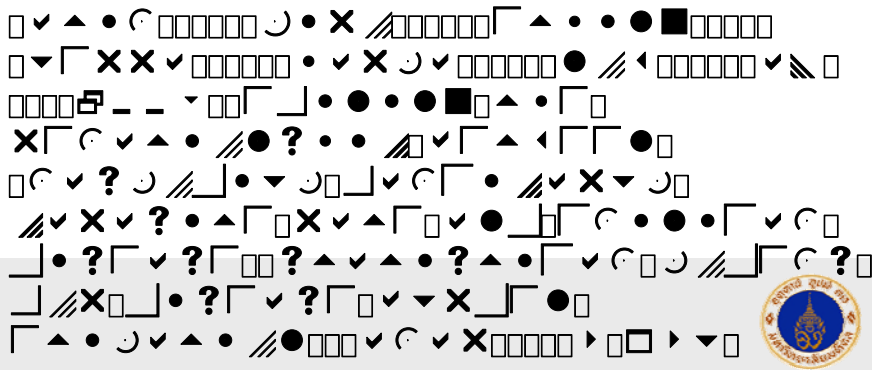
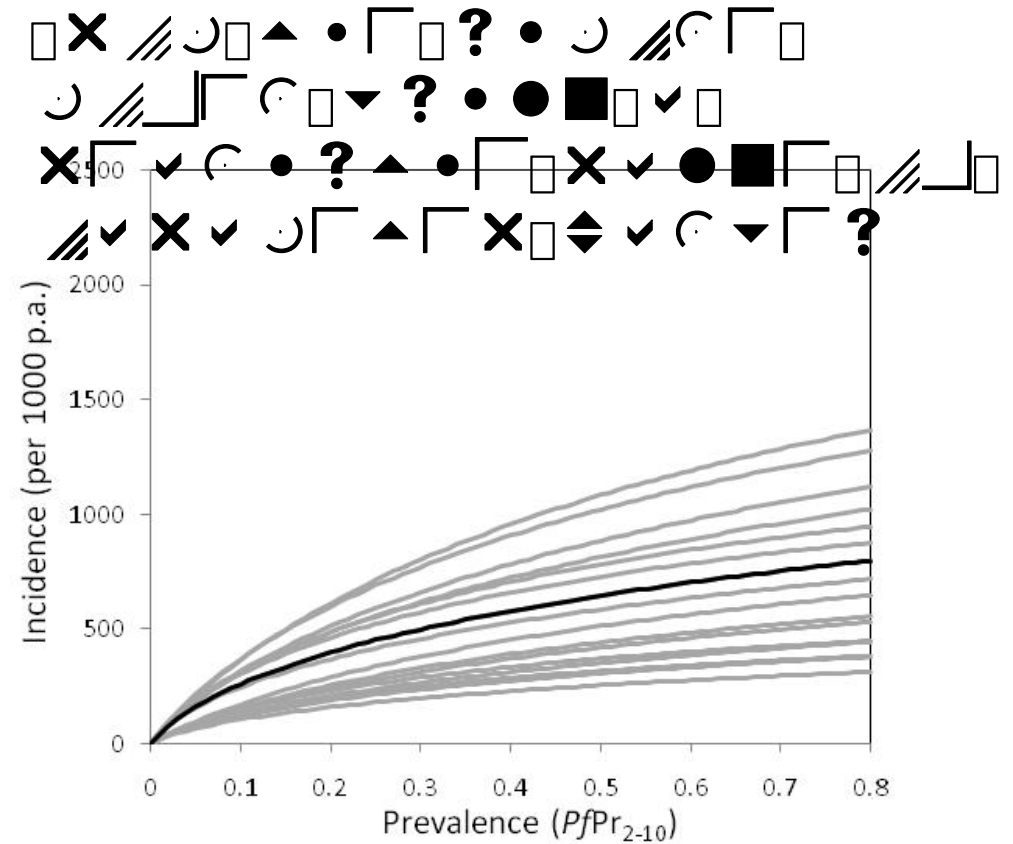
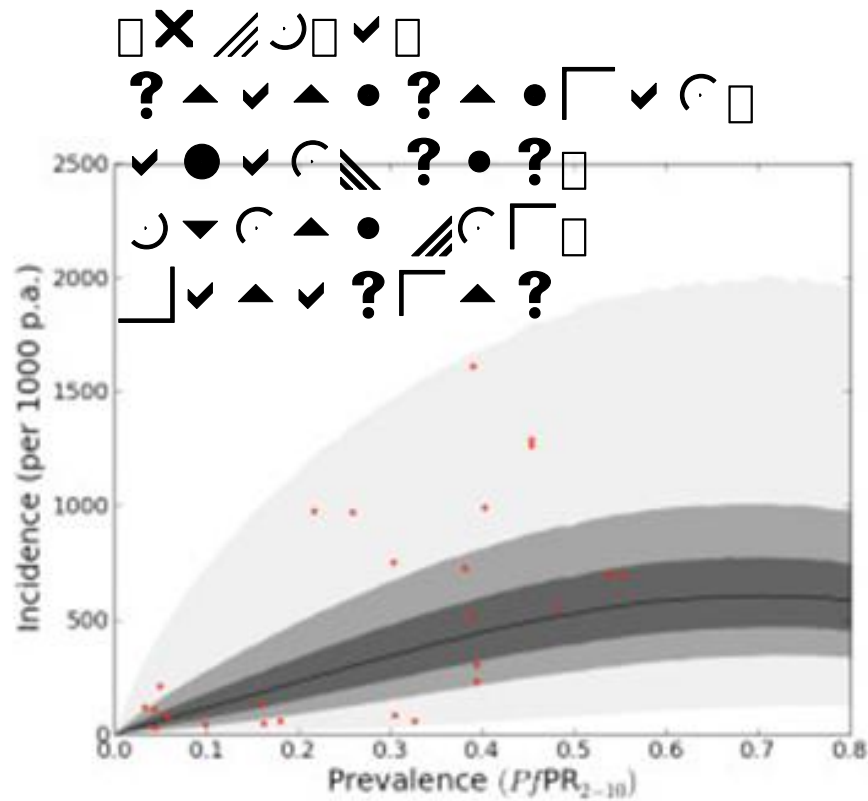
- For a range of transmission intensities the model can:
 - reproduce age profiles of clinical infection in a range of transmission intensities
 - reproduce measured relationship between clinical and sub-clinical infections



Reproducing clinical infection age profiles



Reproducing relationship between parasite prevalence and clinical infection



Elimination model

$$S' = (1 - c_b) \frac{N}{L} - \left(\pi\lambda + \frac{1}{L} \right) S + \frac{1}{d_{imm}} R - x(t)S + yS_v$$

$$I_1' = \pi\lambda S - \left(\frac{\eta p_1 + m}{d_{treat}} + \frac{1}{L} + \frac{1}{d_{treat}} \right) I_1 - x(t)I_1 + yI_{1V} - m(t)I_1$$

$$I_2' = \pi\lambda R - \left(\frac{\eta p_2 + m}{d_{treat}} + \frac{1}{L} + \frac{1}{d_{treat}} \right) I_2 - x(t)I_2 + yI_{2V} - m(t)I_2$$

$$R' = \left(\frac{\eta p_1 + m}{d_{treat}} + \frac{1}{L} + \frac{1}{d_{treat}} \right) I_1 + \left(\frac{\eta p_2 + m}{d_{treat}} + \frac{1}{L} + \frac{1}{d_{treat}} \right) I_2 - \left[\pi\lambda + \frac{1}{d_{imm}} + \frac{1}{L} \right] R - x(t)R + yR_v$$

$$S_v' = c_b \frac{N}{L} - \left(\rho\pi\lambda + \frac{1}{L} \right) S_v + \frac{1}{d_{imm}} R - x(t)S_v + yS_v$$

$$I_{1V}' = \rho\pi\lambda S_v - \left(\frac{\eta p_1 + m}{d_{treat}} + \frac{1}{L} + \frac{1}{d_{treat}} \right) I_{1V} - x(t)I_{1V} + yI_{1V}$$

$$I_{2V}' = \rho\pi\lambda R - \left(\frac{\eta p_2 + m}{d_{treat}} + \frac{1}{L} + \frac{1}{d_{treat}} \right) I_{2V} - x(t)I_{2V} + yI_{2V}$$

$$R_v' = \left(\frac{\eta p_1 + m}{d_{treat}} + \frac{1}{L} + \frac{1}{d_{treat}} \right) I_{1V} + \left(\frac{\eta p_2 + m}{d_{treat}} + \frac{1}{L} + \frac{1}{d_{treat}} \right) I_{2V} - \left[\rho\pi\lambda + \frac{1}{d_{imm}} + \frac{1}{L} \right] R_v - x(t)R_v + yR_v$$

$$\lambda = \frac{R_0 \left(\frac{1}{L} + \frac{1}{d_{treat}} \right)}{C + P}$$

$$C = p_1 (I_1 + I_{1V}) + p_2 (I_2 + I_{2V})$$

$$P = \eta p_1 (I_1 + I_{1V}) + \eta p_2 (I_2 + I_{2V})$$

$$x(t) = \begin{cases} -4 \ln \left(\frac{100 - c}{100} \right) & \text{for } \text{mod}(t, 1) \geq \frac{9}{12} \\ 0 & \text{for } \text{mod}(t, 1) < \frac{9}{12} \end{cases}$$

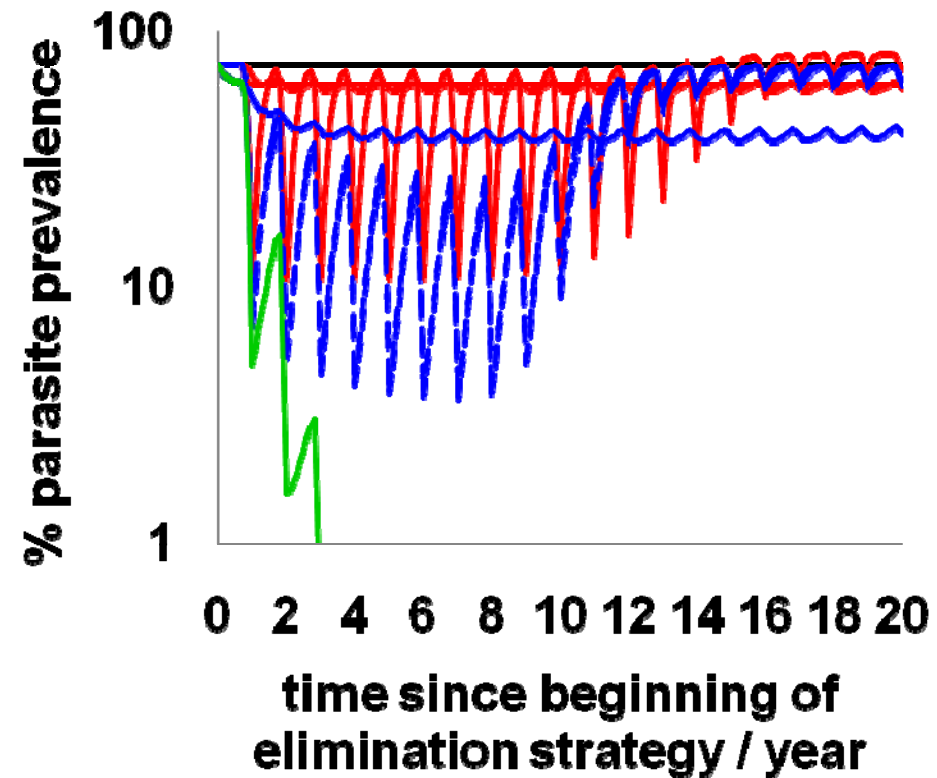
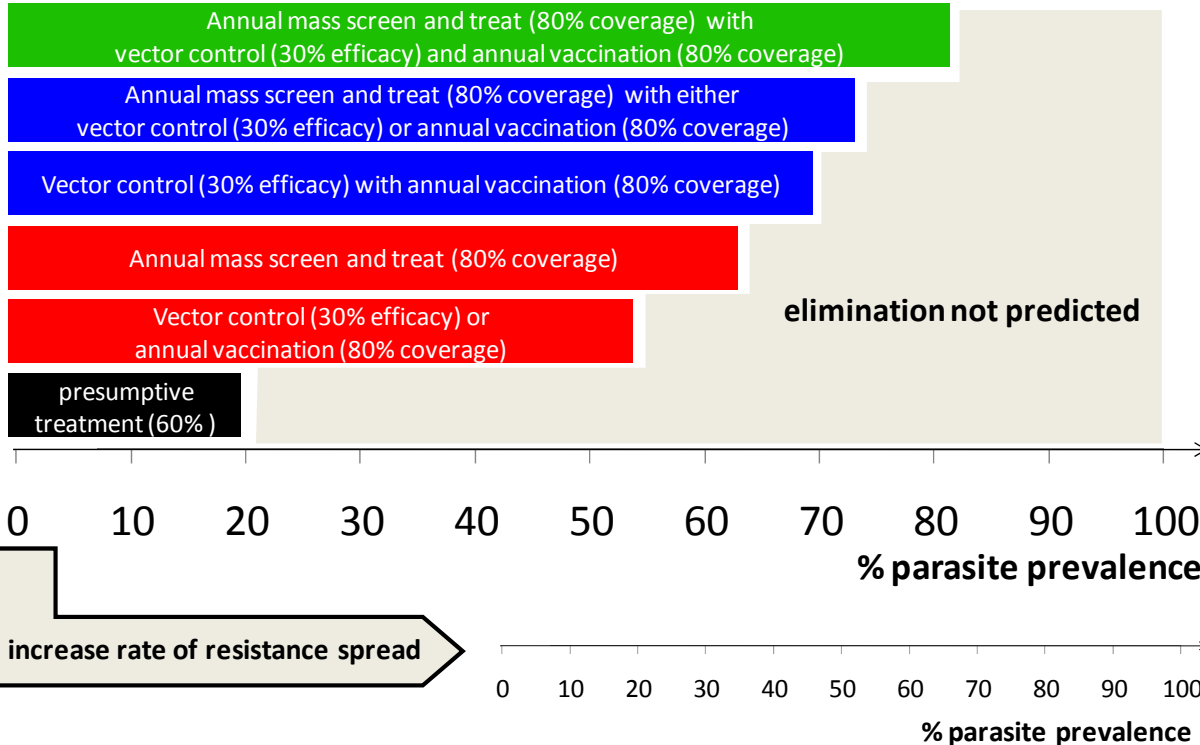
$$m(t) = \begin{cases} \exp \left(-4 \ln \left(\frac{100 - c}{100} \right) \left(t - \frac{9}{12} \right) \right) & \text{for } \text{mod}(t, 1) \geq \frac{9}{12} \\ 0 & \text{for } \text{mod}(t, 1) < \frac{9}{12} \end{cases}$$

- Given annually to all age groups, reaching a coverage of 80% within a three-month period. The method of administration could be similar to or in conjunction with a MSAT programme



Combining strategies

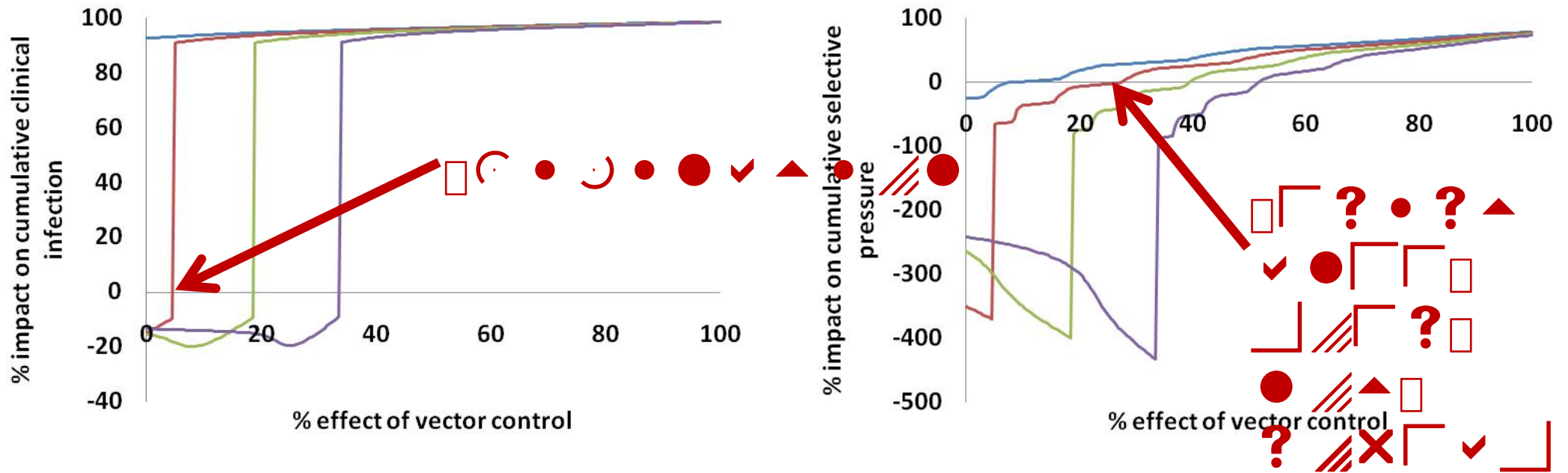
elimination predicted with given strategy



- Combining strategies that seem ineffective independently can result in elimination
- especially if resistance is not spreading



Protecting ACTs

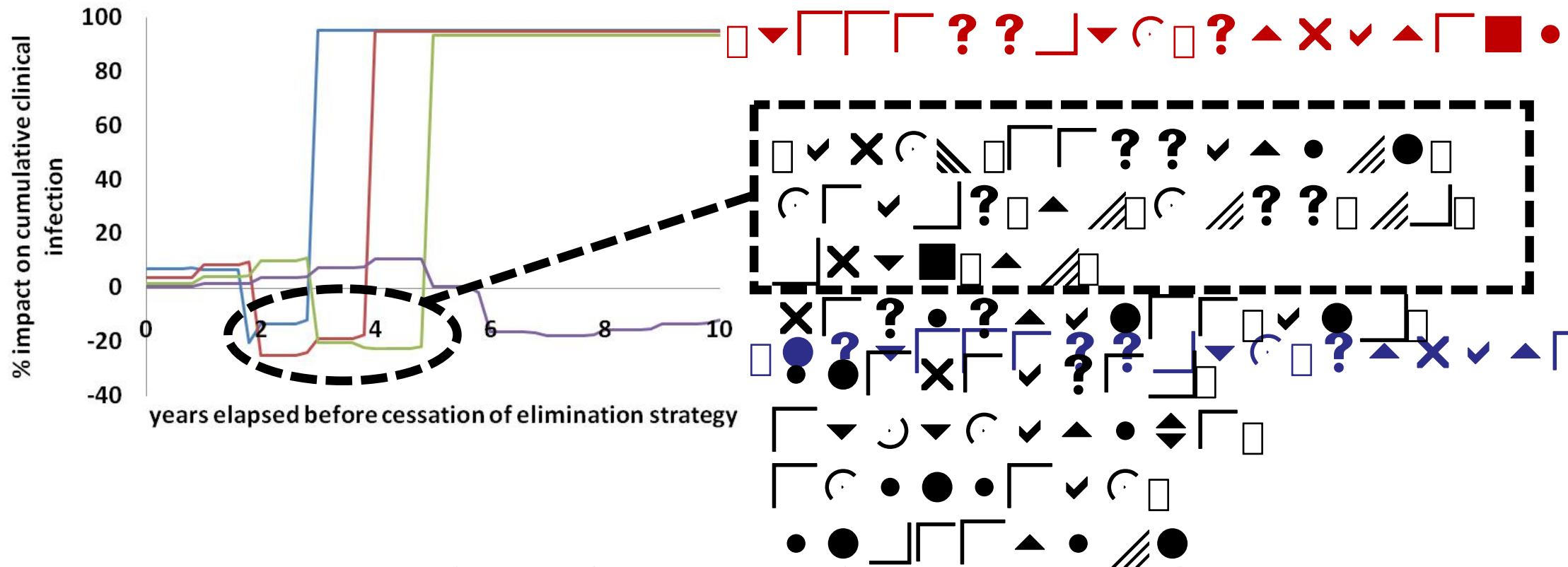


- **Combining strategies at suitable levels can eliminate while protecting against the spread of resistance**



Early cessation of strategy

D



- Early cessation of a potentially successful strategy can have a negative impact on clinical infection if resistance is already spreading



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Future challenges for modelling elimination

- **Simple deterministic models are not up to the job of modelling the final stages of elimination and long term dynamics**
- **Detailed stochastic models are required**
- **These models exist but require**
 - **large, precise and diverse data that are**
 - **geographically explicit**
- **Do we have those data?**



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Acknowledgements

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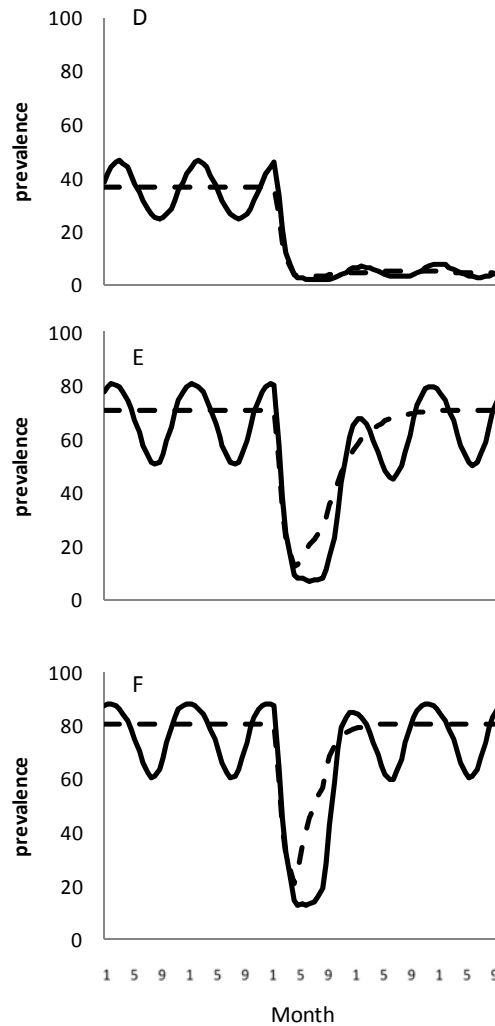
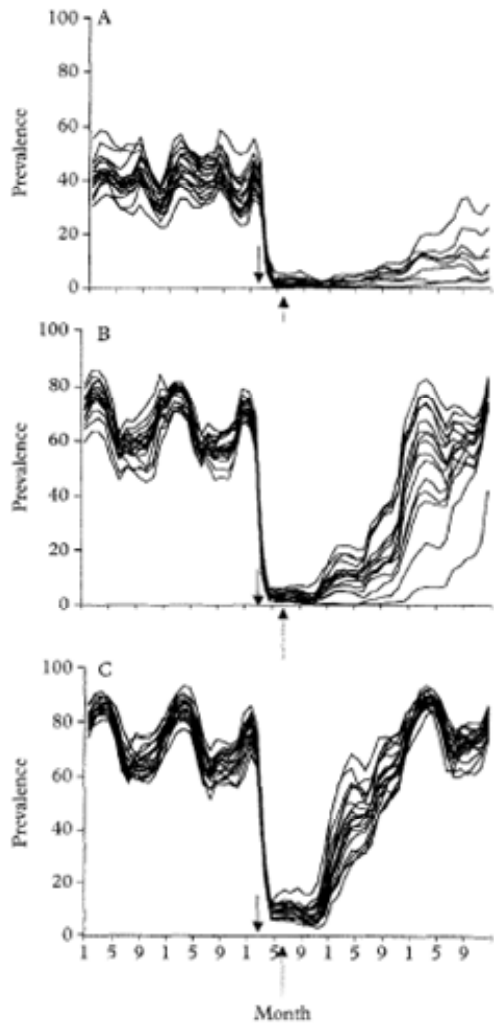
Any questions?



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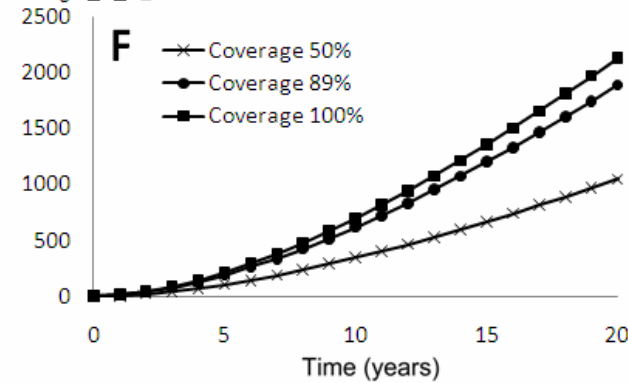
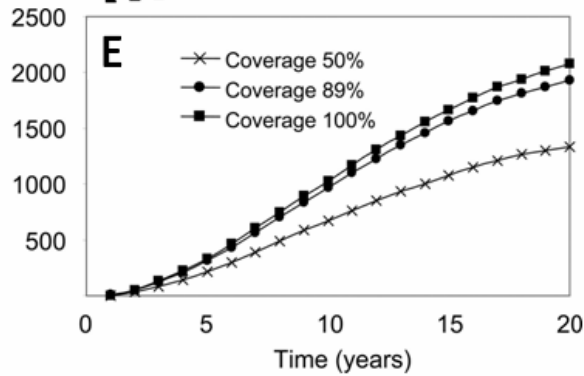
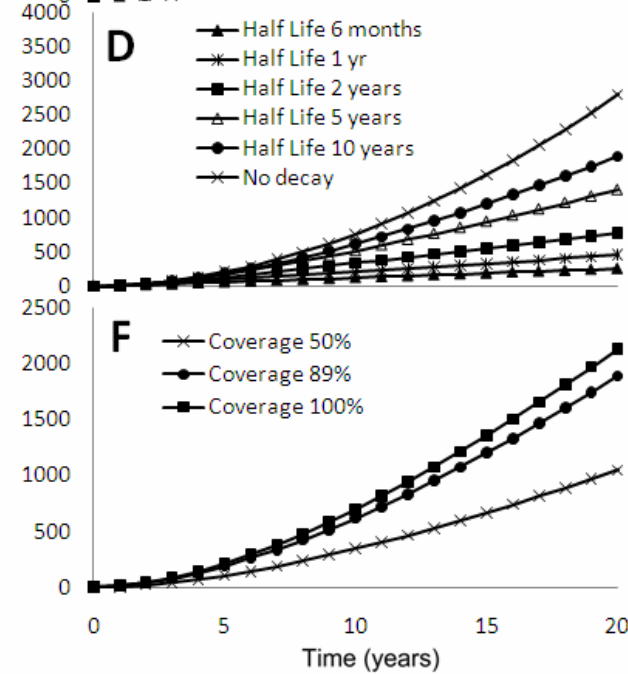
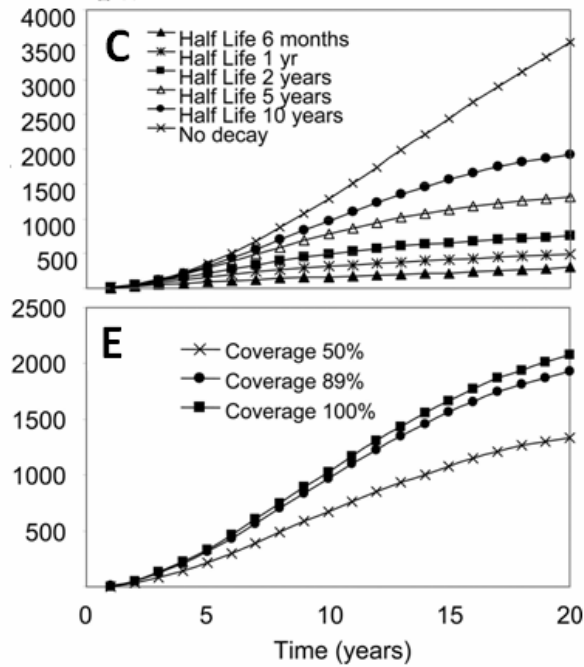
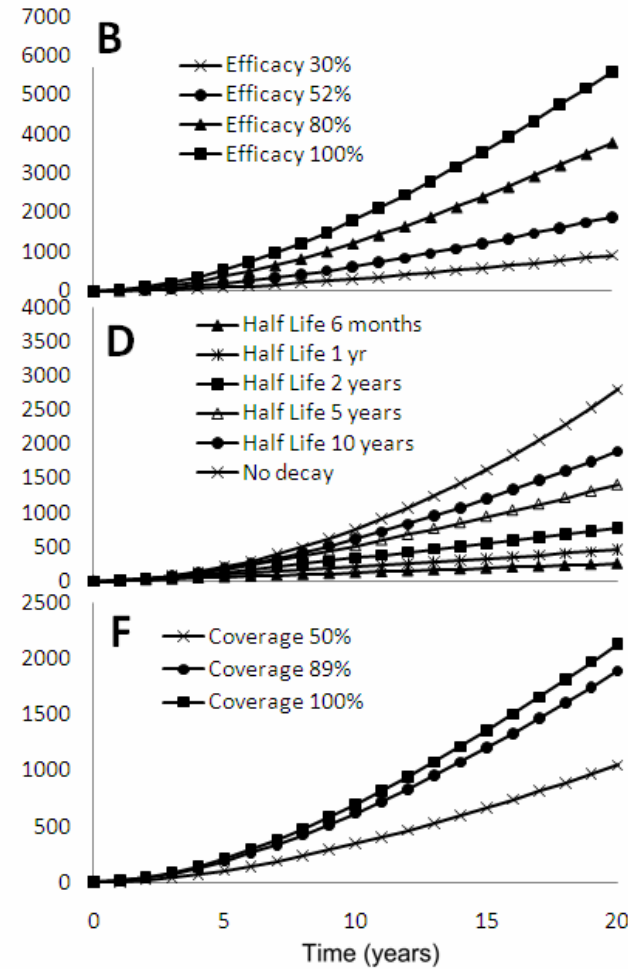
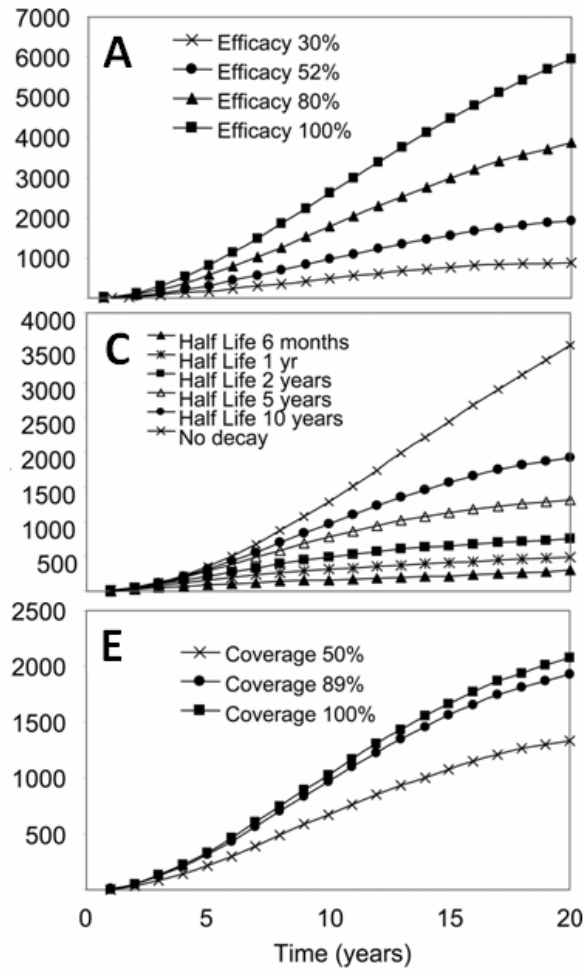
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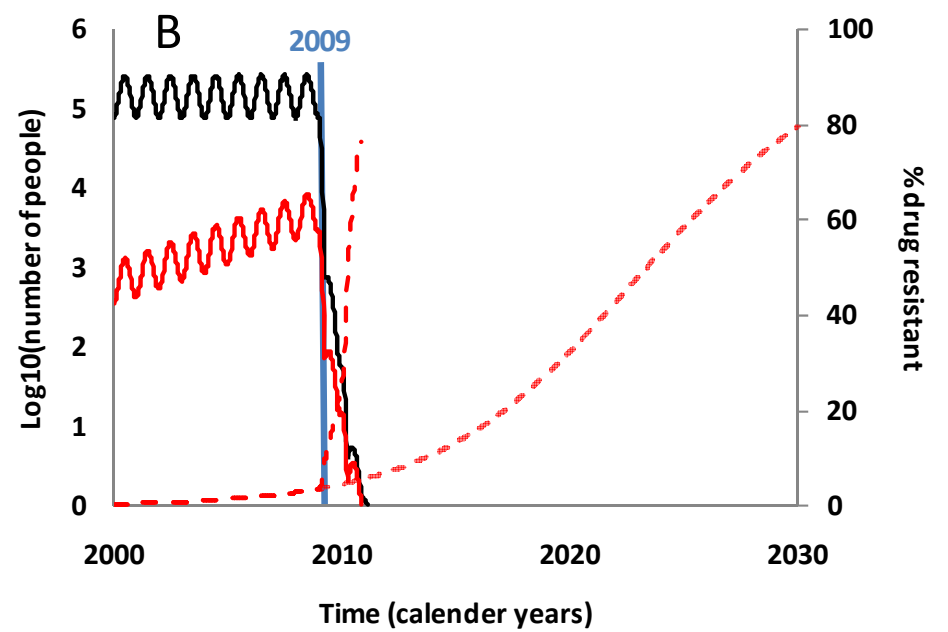
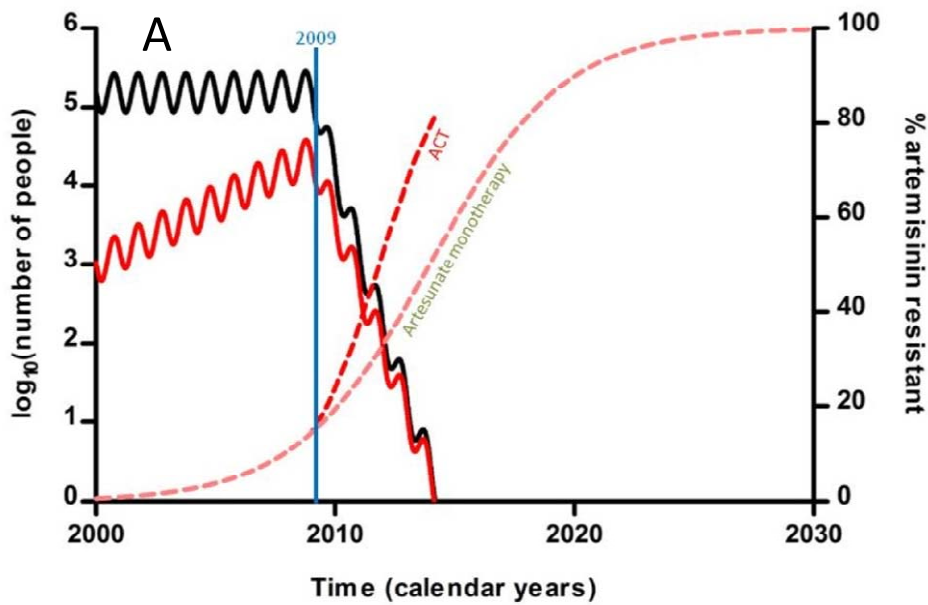


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